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BaB₄O₅F₄ with reversible phase transition featuring unprecedented fundamental building blocks of $[B_{16}O_{21}F_{16}]$ in the α -phase and $[B_4O_6F_4]$ in the β -phase[†]

Wenbin Zhang,‡^{ab} Siru Guo,‡^{ab} Shujuan Han, ^(b)*^{ab} Liying Wang,^c Xin Zhou, ^(b)^c Zhihua Yang ^(b)*^{ab} and Shilie Pan ^(b)*^{ab}

The first fluorooxoborate with reversible phase transition, $BaB_4O_5F_4$, has been obtained. Interestingly, the two polymorphs, α - and β -BaB_4O_5F_4 with rare [BOF_3], feature various one-dimensional chains composed of the unprecedented fundamental building blocks of [B_{16}O_{21}F_{16}] and [B_4O_6F_4], respectively. First-principles calculations were performed to elucidate the structure–property relationships.

With structural versatility, a wide transmittance range, and a high laser damage threshold, borates are the preferred system for probing optical crystals, and they have highly significant applications in semiconductor manufacturing, laser micromachining, photolithography, and other aspects.¹ As the basic structural building blocks of borate, triangular [BO₃] or tetrahedral [BO₄] can be interconnected by sharing O atoms to form different fundamental building blocks (FBBs), such as [B₃O₆] in β -BaB₂O₄,² [B₁₁O₂₂] in Li₆Rb₅(B₁₁O₂₂),³ [B₆₃O₁₃₃] in Cs₃B₇O₁₂,⁴ and [B₄₀O₇₇] in Li₄Cs₄B₄₀O₆₄,⁵ *etc.* Then, the interconnection of each FBB results in the borates exhibiting multiple anionic frameworks: isolated clusters, one-dimensional (1D) infinite chains, 2D layers, or 3D frameworks.⁶ These results greatly enrich the structural chemistry of borates.

Furthermore, the introduction of F atoms with large electronegativity can result in the structural chemistry of borate being

^a CAS Key Laboratory of Functional Materials and Devices for Special Environments, Xinjiang Technical Institute of Physics & Chemistry, CAS, Xinjiang Key Laboratory of Electronic Information Materials and Devices, 40-1 South Beijing Road, Urumqi 830011, China. E-mail: hansj@ms.xjb.ac.cn, slpan@ms.xjb.ac.cn

more abundant, especially as fluorooxoborate with the B-F bond is formed.⁷ In general, F can substitute the O atom in [BO₄] to form [BO₃F], [BO₂F₂], and [BOF₃] groups. Up until now, $[BO_3F]$ and $[BO_2F_2]$ groups have been present in most fluorooxoborates, while $[BOF_3]$ groups are extremely rare. The $[BO_xF_{4-x}]$ (x = 1, 2, and 3) basic units are further interconnected by $[BO_3]$ or [BO₄] to form novel FBBs, such as [B₂O₆F] in BiB₂O₄F,⁸ $[B_4O_8F]$ in AB₄O₆F (A = NH₄, Na, Rb, Cs, K/Cs, or Rb/Cs),⁹ $[B_7O_{13}F_2]$ in Na₃B₇O₁₁F₂,¹⁰ etc., and these further enrich the diversity of the B-O-F anion framework. In addition, F as the terminal atom facilitates breaking of the 3D B-O network structure, resulting in it being more inclined to form various 2D, 1D or isolated structures.¹¹ Moreover, most of the B-O-F anionic frameworks exhibit isolated clusters and 2D layer structures, and only very few of them present 1D chain structures.¹² The 1D chain structure may twist under certain circumstances, producing a phase transition. In addition, polymorphism is of particular interest and is important for developing new functional materials and understanding structure-property relationships, since polymorphism has promising applications in pharmaceuticals, pigments, foods, dyestuffs and so on.¹³ In addition to enriching the structural chemistry, fluorooxoborates have also received much attention in recent years for their excellent performance induced by the $[BO_xF_{4-x}]$ groups. Compared with $[BO_3]$ and $[BO_4]$, the larger hyper-polarizability tensor and highest occupied molecular orbital-lowest unoccupied molecular orbital (HOMO-LUMO) gaps of the $[BO_xF_{4-x}]$ groups can result in enhanced anisotropy, as well as blue-shift the cut-off edge.14 Fluorooxoborate is one of the prominent research topics in the exploration of new deep ultraviolet (DUV) optical crystals.

In this communication, we have discovered the first case among alkaline earth metal fluorooxoborates to exhibit reversible phase transition, $P2_1$ for α -BaB₄O₅F₄, and $P2_1/c$ for β -BaB₄O₅F₄ (α and β correspond to low and high temperature phases, respectively). α -BaB₄O₅F₄ and β -BaB₄O₅F₄ exhibit 1D chains composed of unprecedented FBBs, [B₁₆O₂₁F₁₆] and [B₄O₆F₄], respectively. The crystallographic data and details of

^b Center of Materials Science and Optoelectronics Engineering, University of Chinese Academy of Sciences, Beijing 100049, China

^c Key Laboratory of Magnetic Resonance in Biological Systems, State Key Laboratory of Magnetic Resonance and Atomic and Molecular Physics,

National Center for Magnetic Resonance in Wuhan, Wuhan Institute of Physics and Mathematics, CAS, Wuhan 430071, P. R. China

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[‡] These authors contributed equally to this work.



Fig. 1 The calculated powder X-ray diffraction patterns for α - and β -BaB₄O₅F₄, and the experimental powder X-ray diffraction patterns for β -BaB₄O₅F₄.

the structural refinement of α - and β -BaB₄O₅F₄ are provided in Tables S1–S4 in the ESI.†

Single crystal X-ray diffraction revealed that the two new compounds crystallized into the space groups of $P2_1$ (No. 4) and $P2_1/c$ (No. 14), respectively (Table S5, ESI†). Relatively low temperature and the residual factor validated models of these two crystals indicated the presence of two polymorphs. By comparing the standard XRD of the BaB₄O₅F₄ polymorphs, it is clear that the theoretical XRD pattern of α -BaB₄O₅F₄ has one obvious peak at $2\theta = 13.5^{\circ}$ (Fig. 1). The polycrystalline sample of β -BaB₄O₅F₄ was obtained at 450 °C in the closed system. In order to further explore the temperature of its phase transition, the polycrystalline sample was tested using a Bruker SMART APEX II CCD under the temperatures of 295, 250, 220, 200, and 190 K (Fig. S1, ESI†). β -BaB₄O₅F₄ was stable from room temperature to 220 K, and then it begins to change into α -BaB₄O₅F₄

in the temperature range from 220 to 190 K. When the temperature begins to rise, the α -BaB₄O₅F₄ phase can also change into β -BaB₄O₅F₄ (the appearance of the X-ray diffraction peaks at about $2\theta = 13.5^{\circ}$ can help us to judge this phase transition), indicating the reversibility of this phase transition.

 α -BaB₄O₅F₄ crystallizes in the monoclinic space group P2₁ with four unique barium sites, sixteen unique boron sites, twenty unique oxygen sites, and sixteen unique fluorine sites in the asymmetric structure unit. β -BaB₄O₅F₄ crystallizes in the centrosymmetric space group, $P2_1/c$. There are one, four, five, and four crystallographically-independent atom numbers for Ba, B, O, and F in the asymmetric structure unit, respectively. Both α and β -BaB₄O₅F₄ exhibit a 3D framework composed of $[BO_3]$, $[BO_3F]$, $[BOF_3]$ and $[BaO_5F_6]$ groups. In α -BaB₄O₅F₄, four $[B_3O_6F]$ rings are linked together by sharing vertex O atoms to form a [B₁₂O₂₁F₄] short chain, which further connects four $[BOF_3]$ units to build its FBB, $[B_{16}O_{21}F_{16}]$. Then, the FBBs are linked together to construct the 1D $[B_{16}O_{20}F_{16}]_\infty$ chains, and the Ba cations are sequentially distributed among the chains to maintain the structural balance (Fig. 2b). Compared with α -BaB₄O₅F₄, β -BaB₄O₅F₄ features different 1D [B₄O₅F₄]_{∞} chains that are separated by Ba atoms, and its FBB is $[B_4O_6F_4]$ composed of one [B3O6F] unit and one [BOF3] unit. The structural difference between α - and β -BaB₄O₅F₄ is shown in Fig. 2, there are four types of $[BOF_3]$ in α -BaB₄O₅F₄, and only one unique [BOF₃] group in β -BaB₄O₅F₄. It can clearly be observed that the four types of [BOF₃] tetrahedra are arranged alternately in the chain, which shows the different orientations in α -BaB₄O₅F₄, while the [BOF₃] groups in β -BaB₄O₅F₄ are arranged in two directions along the c-axis. As shown in Fig. S2 (ESI[†]), in α -BaB₄O₅F₄, the [B₁₆O₂₀F₁₆] $_{\infty}$ chain can generate itself only by 2₁-screw axes. For β -BaB₄O₅F₄, as well as the 2₁-screw axes, a glide plane is added, seen from the a-axes, the BO_3F group (1) operates itself by a mirror symmetrical



Fig. 2 The crystal structure features of BaB₄O₅F₄. (a and d) The FBB of α - and β -BaB₄O₅F₄. (b, c, e and f) The structure differences between α - and β -BaB₄O₅F₄.

operation, and then shifts a distance of c/2 to generate the BO₃F group (2). Eventually, β -BaB₄O₅F₄ crystallizes in the $P2_1/c$ symmetry group.

In α -BaB₄O₅F₄, the B (1, 2, 5, 10, 12, 13, 15, and 16) atoms are coordinated with three O atoms, forming [BO₃] units with B–O bond lengths varying from 1.291 to 1.412 Å, respectively, while B (3, 6, 11, and 14) atoms and B (4, 7, 8, and 9) atoms are located in the four-coordination environment to form the [BO₃F] and [BOF₃] units, respectively (the B–F bond lengths vary from 1.363 to 1.457 Å). However, in β -BaB₄O₅F₄, B(1 and 4)O₃, B(2)O₃F and B(3)OF₃ are connected, resulting in a sixmembered ring structure, [B₄O₆F₄] (Fig. 2d). The B–O bond lengths are in the range of 1.353–1.458 Å, and the B–F bond lengths range from 1.364 to 1.432 Å, which are consistent with the previously reported results in the borate system.

In addition, the Ba cations are coordinated with five O atoms and six F atoms to form $[BaO_5F_6]$ polyhedra in α - and β -BaB₄O₅F₄. Due to the change in the B–O–F chains, there is also a difference in the arrangement of cations. In α -BaB₄O₅F₄, the Ba(1)–O chain, which is formed by $Ba(1)O_5F_6$, further links with the Ba(2)-O chain by sharing F atoms, to give the Ba-O-F double chain, and the Ba (3 and 4) cations also exhibit the same arrangement. Compared with α -BaB₄O₅F₄, the unique [BaO₅F₆] polyhedron is connected with each other by sharing F atoms to form a 1D single chain in β -BaB₄O₅F₄ (Fig. 2f). In addition, the calculated bond valence sum (BVS) values of these atoms are shown in Tables S1 and S3 (ESI[†]),¹⁵ and these values are within the allowable range, proving the accuracy of the structures. The Global Instability Index (GII) was also calculated,¹⁶ which is derived from the bond valence concepts and can be used to evaluate the rationality of structures. Values greater than 0.05 valence units (vu) indicate that the structure is strained, whereas values greater than 0.20 vu indicate that the strain is so great that the structure is unstable. The calculated GII values of α - and β -BaB₄O₅F₄ are in the range of 0.089–0.093 vu (Table 1). The values of bond valence and GII for the two compounds are reasonable, suggesting that the crystal structures of these compounds are reasonable.

It is worth noting that the FBBs of α - and β -BaB₄O₅F₄ have never been reported in previously reported fluorooxoborates. To the best of our knowledge, 21 different FBBs have been reported in fluorooxoborates,^{12*c*,17} the title compounds were firstly discovered with [BOF₃] groups in the fluorooxoborate without the hydroxyl, and [BOF₃] groups were also found in Ba(B₂OF₃(OH)₂)₂.¹⁸ In addition, the FBBs of other fluorooxoborates with four B atoms in the molecular formula, AB₄O₆F (A = NH₄ and alkali metal), AB₄O₆F₂ (A = Ca, Sr, and Ba),¹⁹

Table 1 The calculated Global Instability Index (GII) values for $\alpha\text{-}$ and $\beta\text{-}BaB_4O_5F_4$

	Bond valence sum				
BaB ₄ O ₅ F ₄	Ва	В	0	F	GII
α- β-	2.02-2.18 2.15	2.87-3.13 3.01-3.13	1.91–2.14 1.99–2.09	0.81-1.09 0.9-1.14	0.093 0.089

and KNiB₄O₆F₃,²⁰ were composed of [BO₃] and [BO₃F], as listed in Fig. S3 (ESI[†]). All of these FBBs form 2D B–O–F anion layered structures. Furthermore, from a molecular formula point of view, BaB₄O₅F₄ can be seen as two F atoms replacing one O atom in BaB₄O₆F₂. As more fluorine atoms are introduced into the structure, some of them as terminal atoms could break the original 18-membered ring in the BaB₄O₆F₂ structure, as a scissor. Then, the layered framework (2D) is destroyed, to form the chain (1D) in BaB₄O₅F₄, thereby further enriching the diversity of fluorooxoborate structures.

In order to confirm the presence of F atoms, energy dispersive X-ray spectroscopy (EDS) was carried out on the clean single crystal surface, and the results revealed the presence of F and O atoms in BaB₄O₅F₄ (Fig. S4, ESI[†]). Solid state Nuclear Magnetic Resonance (NMR) spectroscopy was carried out to verify the existence of B-F bonds. In the 19F MAS NMR spectrum, the signals at -120.1 and -122.2 ppm were assigned to the F atoms in the B–F groups (Fig. 3a).^{18,21} For the ¹¹B MAS NMR spectrum, according to previous work, the broad signals within the range of 5 to 15 ppm can be assigned to the chemical shifts of BO₃ units, and the narrow signals around 0 ppm can be assigned to the tetrahedral coordinated B atoms.²² The ¹¹B{¹⁹F}-rotational echo double resonance (REDOR) experiments were performed to establish the B-F bonds for the tetrahedral [BO3F] and [BOF3] units, and the differences in the obtained spectra are shown in Fig. 3c, which clearly indicates the existence of tetrahedrally coordinated B nuclei with B-F bonds in β -BaB₄O₅F₄. The IR spectrum of the β -BaB₄O₅F₄ compound is shown in Fig. S5 (ESI[†]). The peak assignments are comparable to those of previously reported fluorooxoborates, proving the correctness and reliability of the structure. The UV-vis-NIR diffuse-reflectance data was collected for the as-synthesized β -BaB₄O₅F₄ compound, and the data indicated that the compound has a wide transparent region and the bandgap is larger than 6.72 eV (Fig. S6, ESI⁺).

To investigate the relationship between the structure and properties of α - and β -BaB₄O₅F₄, calculations were performed using first principles. The calculated band structures with GGA showed indirect band gaps of 6.83 and 6.79 eV for α - and β -BaB₄O₅F₄, respectively (Fig. S7a and b, ESI†).²³ To ensure the accuracy and the consistency of the band gaps, considering the discontinuity of the exchange-related energy function, the



Fig. 3 ${}^{11}B$, ${}^{19}F$, and ${}^{11}B{}^{19}F$ -REDOR MAS NMR spectra of β -BaB₄O₅F₄.

Heyd-Scuseria-Ernzerhof (HSE06) hybrid DFT function was also used for the calculations.²⁴ According to the calculation results, the band gaps of α - and β -BaB₄O₅F₄ using the HSE06 function were 8.40 and 8.30 eV, respectively, meaning that the title compounds are of greater application in the DUV region. The main reasons for having large band gaps of α - and β -BaB₄O₅F₄ are as follows: (1) all the elements of BaB₄O₅F₄ are free of *d*-*d* or *f*-*f* electronic transitions; (2) the introduction of more F atoms facilitates the increase in a large band gap. In addition, in order to investigate the reasons for having a large band gap, the partial densities of states (PDOS) were calculated from the point of the intrinsic relationship between the electronic structure and the properties (Fig. S7c and d, ESI⁺). From -6 eV to the top of the valence band, it is dominated by O 2p states, F 2p states and B 2p states, whilst the bottom of the conduction band is dominated by B 2p states, Ba 5d states and a small amount of O 2p states. Therefore, the B-O-F and Ba-O interactions play a decisive role in determining the band gap of the title compounds. The calculated birefringence values of α - and β -BaB₄O₅F₄ at 1064 nm were shown to be 0.044 and 0.047, respectively, using first-principles calculations (Fig. S8, ESI⁺).

In summary, the first case with reversible phase transition in the fluorooxoborate family, BaB4O5F4, has been successfully synthesized in a closed vacuum environment. It features unprecedented FBBs, $[B_{16}O_{21}F_{16}]$ in the α phase and $[B_4O_6F_4]$ in the β phase, constructing the 1D $[B_{16}O_{20}F_{16}]_{\infty}$ and $[B_4O_5F_4]_{\infty}$ chains, respectively. BaB₄O₅F₄ has a large band gap and moderate birefringence, indicating that it has good application prospects in the DUV region.

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Conflicts of interest

There are no conflicts to declare.

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